



## WYDZIAŁ MATEMATYCZNO – FIZYCZNY Instytut Matematyki

Zaprasza na wykład pod tytułem:

### FUNCTIONAL EQUATIONS ON DOUBLE COSET HYPERGROUPS.

który wygłosi:

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#### ABSTRACT:

Let  $K$  be a locally compact Hausdorff topological space. Hypergroups are algebras with involutions of all complex valued bounded Radon measures on  $K$  with some additional properties. We are going to study a particular class of hypergroups, namely double coset hypergroup.

Let  $G$  be a locally compact group with identity  $e$  and  $K$  a compact subgroup with normed Haar measure  $\omega$ :  $\int_K d\omega(K) = 1$ . For each  $x$  in  $G$  we define the double coset of  $x$  as the set  $KxK = \{kxl: k, l \in K\}$ .

We introduce a hypergroup structure on the set  $L$  of all double cosets: the topology of  $L$  is the factor topology, which is locally compact. The identity  $o$  is the coset  $K = KeK$  itself and the involution is defined by  $(KxK)^v = Kx^{-1}K$ .

Finally, the convolution of  $\delta_{KxK}$  and  $\delta_{KyK}$  is defined by

$$\delta_{KxK} * \delta_{KyK} = \int_K \delta_{KxkyK} d\omega(k).$$

It is known that this gives a hypergroup structure on  $L$  which is non-commutative, in general. If  $K$  is a normal subgroup, then  $L$  is isomorphic to the hypergroup arising from the factor group  $G/K$ . We describe the complex valued solutions defined on a double coset hypergroup of the exponential, additive and quadratic functional equations. Moreover, the  $m$ -sine functions on a double coset hypergroup are discussed. The double coset hypergroup we consider is closely related to affine groups and spherical functions on them.

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